Write your name here


## Mathematics

## Area and Perimeter: Arcs Sectors Circles

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided - there may be more space than you need.
- You must show all your working.
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- If your calculator does not have a $\pi$ button, take the value of $\pi$ to be 3.142 unless the question instructs otherwise.


## Information

- The total mark for this paper is $\mathbf{7 1}$. There are 16 questions.
- Questions have been arranged in an ascending order of mean difficulty, as found by all students in the June 2017-November 2019 examinations.
- The marks for each question are shown in brackets - use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.


## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

1 The diagram shows a shape made from a trapezium $A B C D$ and a semicircle with diameter $D C$.

$D C=8 \mathrm{~cm}$.
The shape has area $64 \mathrm{~cm}^{2}$
The height of the trapezium is 5 cm .
Work out the length of $A B$.
Give your answer correct to 1 decimal place.
cm

## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

2 The diagram shows a cycle track.


The track has two straight sides each of length 40 m .
Each end of the track is a semicircle of radius 27 m .
The diameter of each wheel of Ian's bike is 590 mm . Ian is going to ride his bike around the track once.

Calculate how many complete revolutions each wheel of his bike will make.
$3 \quad O A B$ is a sector of a circle with centre $O$ and radius 7 cm .


The area of the sector is $40 \mathrm{~cm}^{2}$
Calculate the perimeter of the sector.
Give your answer correct to 3 significant figures.

## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

4

$O N Q$ is a sector of a circle with centre $O$ and radius 11 cm .
$A$ is the point on $O N$ and $B$ is the point on $O Q$ such that $A O B$ is an equilateral triangle of side 7 cm .

Calculate the area of the shaded region as a percentage of the area of the sector $O N Q$. Give your answer correct to 1 decimal place.

5 A square, with sides of length $x \mathrm{~cm}$, is inside a circle.
Each vertex of the square is on the circumference of the circle.
The area of the circle is $49 \mathrm{~cm}^{2}$.
Work out the value of $x$.
Give your answer correct to 3 significant figures.

6 The circumference of circle $\mathbf{B}$ is $90 \%$ of the circumference of circle $\mathbf{A}$.
(a) Find the ratio of the area of circle $\mathbf{A}$ to the area of circle $\mathbf{B}$.

Square $\mathbf{E}$ has sides of length $e \mathrm{~cm}$.
Square $\mathbf{F}$ has sides of length $f \mathrm{~cm}$.
The area of square $\mathbf{E}$ is $44 \%$ greater than the area of square $\mathbf{F}$.
(b) Work out the ratio $e: f$

## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

7 The diagram shows a circle and an equilateral triangle. One side of the equilateral triangle is a diameter of the circle.
The circle has a circumference of 44 cm .
Work out the area of the triangle.
Give your answer correct to 3 significant figures.

. $\mathrm{cm}^{2}$

## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

8 The diagram shows 3 identical circles inside a rectangle.
Each circle touches the other two circles and the sides of the rectangle, as shown in the diagram.


The radius of each circle is 24 mm .
Work out the area of the rectangle.
Give your answer correct to 3 significant figures.
$\mathrm{mm}^{2}$

## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

9 The diagram shows a square $A B C D$ with sides of length 20 cm . It also shows a semicircle and an arc of a circle.

$A B$ is the diameter of the semicircle.
$A C$ is an arc of a circle with centre $B$.
Show that $\frac{\text { area of shaded region }}{\text { area of square }}=\frac{}{8}$

## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

10 Here is a shaded shape $A B C D$.


The shape is made from a triangle and a sector of a circle, centre $O$ and radius 6 cm . $O C D$ is a straight line.
$A D=14 \mathrm{~cm}$
Angle $A O D=140^{\circ}$
Angle $O A D=24^{\circ}$
Calculate the perimeter of the shape.
Give your answer correct to 3 significant figures.

## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

11 The diagram shows a logo made from three circles.


Each circle has centre $O$.
Daisy says that exactly $\frac{1}{3}$ of the logo is shaded.
Is Daisy correct?
You must show all your working.

## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

12 The region $\mathbf{R}$, shown shaded in the diagram, is the region between two circles with the same centre.


The outer circle has radius $(2 n+6)$
The inner circle has radius $(n-1)$
All measurements are in centimetres.
The area of $\mathbf{R}$ is greater than the area of a circle of radius $(n+13) \mathrm{cm}$.
$n$ is an integer.
Find the least possible value of $n$.
You must show all of your working.

13

$A B$ is a chord of a circle centre $O$.
The radius of the circle is 30 cm .
Angle $A O B=80^{\circ}$
Work out what percentage of the area of the circle is shaded.
.

## 1MA1 Higher themed papers: Area and Perimeter - Arcs Sectors Circles

14 The diagram shows a sector of a circle of radius 9 cm .


The sector has a perimeter of 25 cm .
Work out the value of $x$.
Give your answer correct to 1 decimal place.

$O A C$ is a sector of a circle, centre $O$, radius 10 m .
$B A$ is the tangent to the circle at point $A$.
$B C$ is the tangent to the circle at point $C$.
Angle $A O C=120^{\circ}$
Calculate the area of the shaded region.
Give your answer correct to 3 significant figures.

16 Here are two solid prisms, prism $\mathbf{A}$ and prism B.

prism A

prism B

The cross section of prism $\mathbf{A}$ is a sector, with angle $45^{\circ}$, of a circle of radius 10 cm . The prism has a depth of 10 cm and a mass of $40 \pi$ grams.

The cross section of prism $\mathbf{B}$ is a sector, with angle $60^{\circ}$, of a circle of radius 10 cm . The prism has a depth of 5 cm and a mass of $50 \pi$ grams.

Express the difference in the densities of the two prisms as a percentage of the density of prism A.
\%

